

Cosmological constraints from weak lensing, SNIa, and CMB, and Bayesian model selection

Martin Kilbinger
Institut d'Astrophysique de Paris
France



Institut d'Astrophysique de Paris



1st GCOE International Symposium
Sendai, Japan



Tohoku University GCOE program

"Weaving Science Web beyond Particle-Matter Hierarchy"

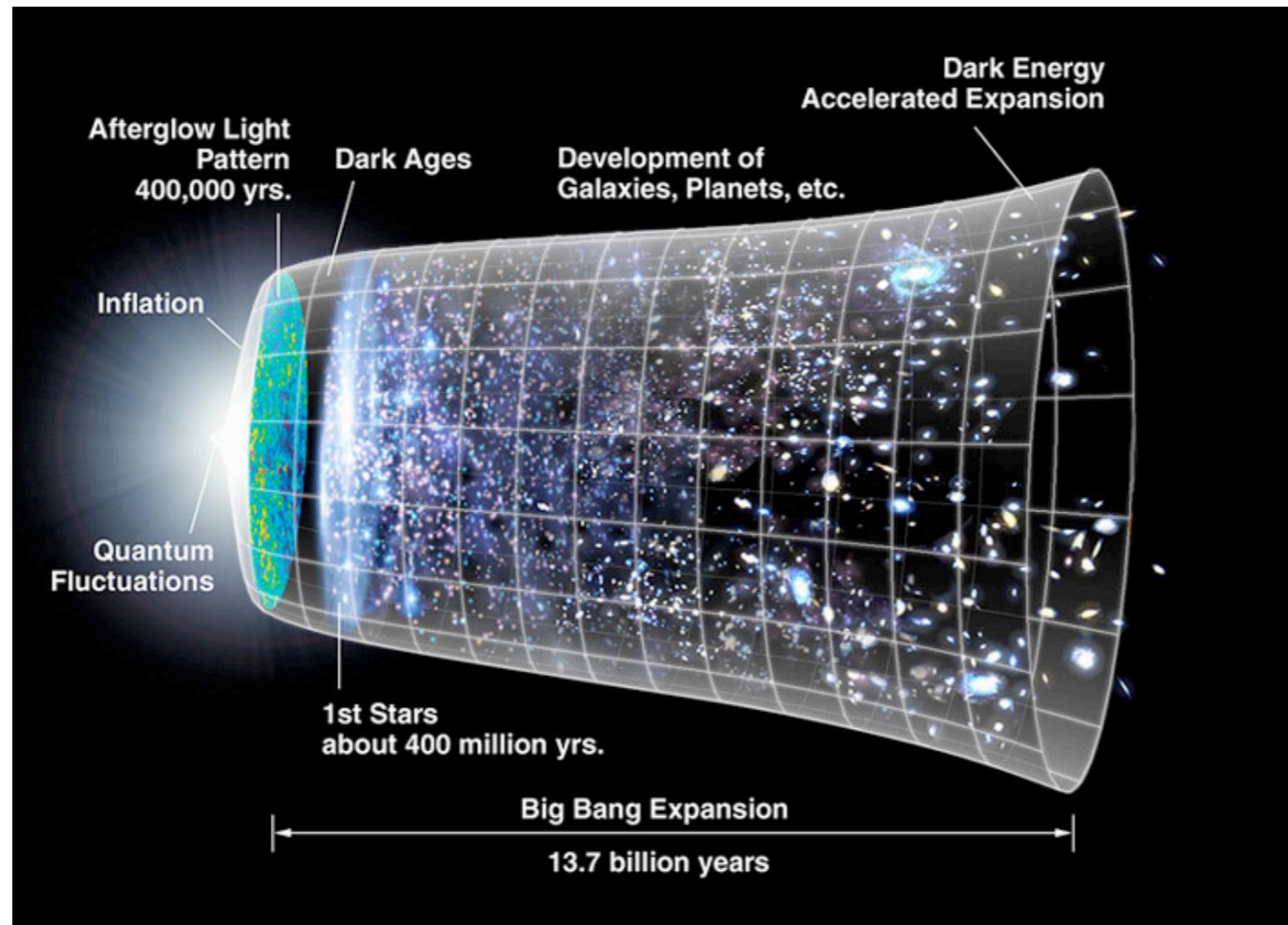
<http://www.scienceweb.tohoku.ac.jp/>

March 5 - 7, 2009

Outline

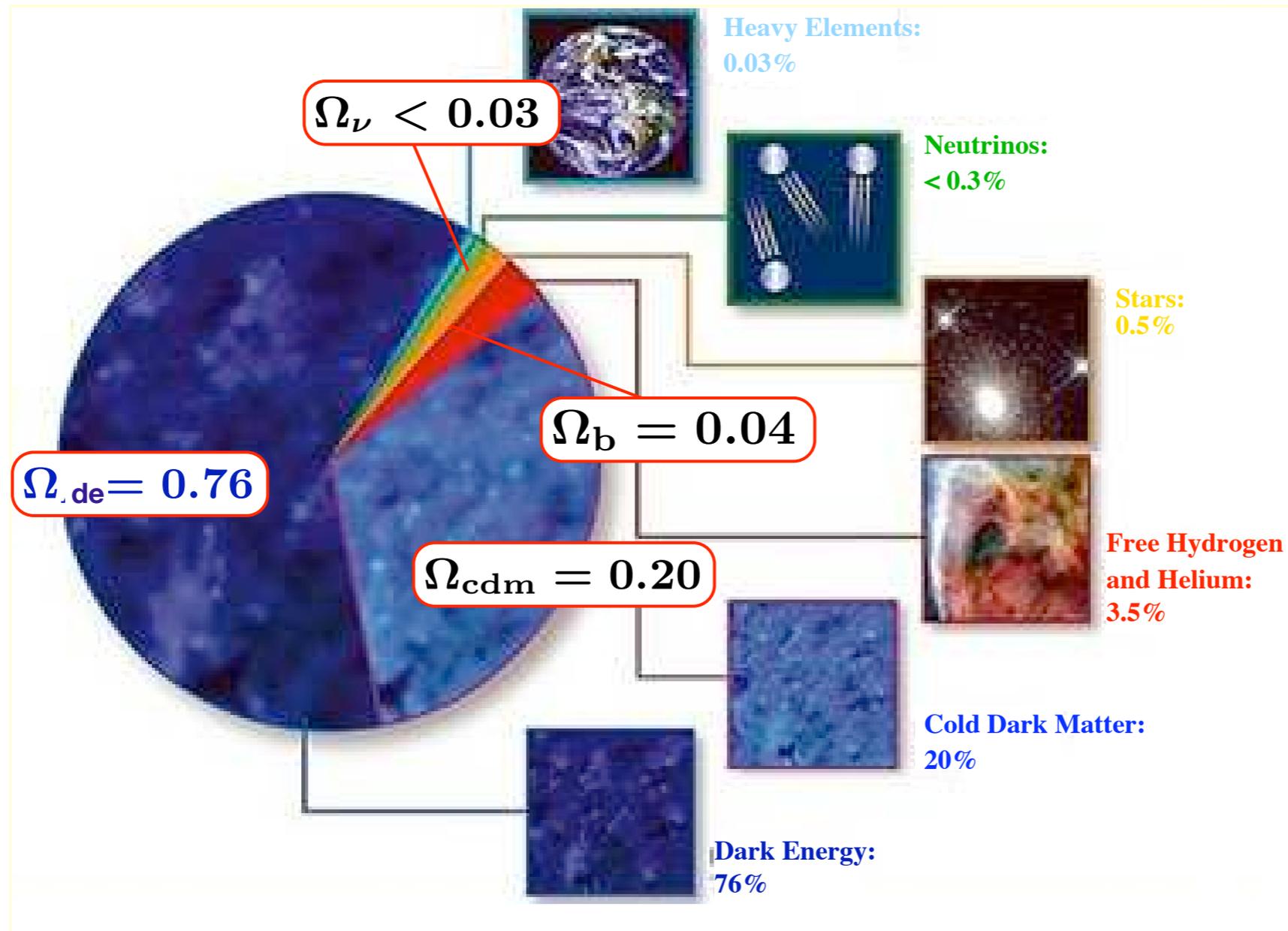
- Cosmology from Cosmic Microwave Background, weak gravitational lensing, and Supernovae type Ia
- Systematics in SNIa: photometric accuracy, dust reddening
- Model selection and Bayesian evidence
- A new method to sample the parameter space and compute the Bayesian evidence
- Results for model selection

Questions in cosmology



- How did the Universe begin, how does it evolve?
- What is it made of?
- How do structures form? (Dark matter, halos, galaxies, ...)

Composition of the Universe



density parameters $\Omega_i \equiv \rho_i / \rho_c$
 critical density: $\rho_c = 3H_0^2 / (8\pi G) = 10^{-29} \text{ g cm}^{-3}$
 total matter density: $\Omega_m = \Omega_{cdm} + \Omega_b$

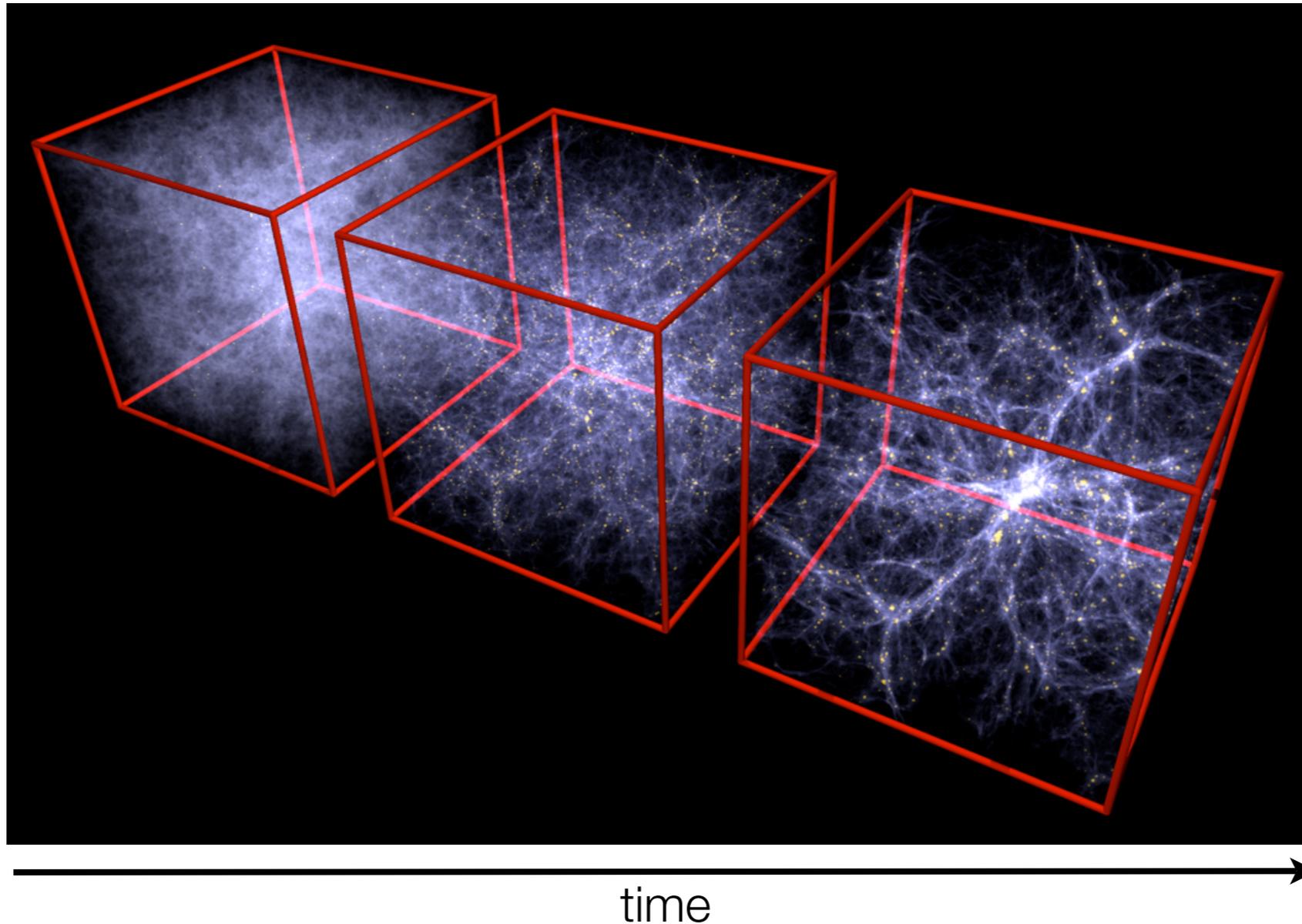
Dark energy or cosmological constant?

$$w = p / (\rho c^2)$$

$$w \neq -1$$

$$w = -1$$

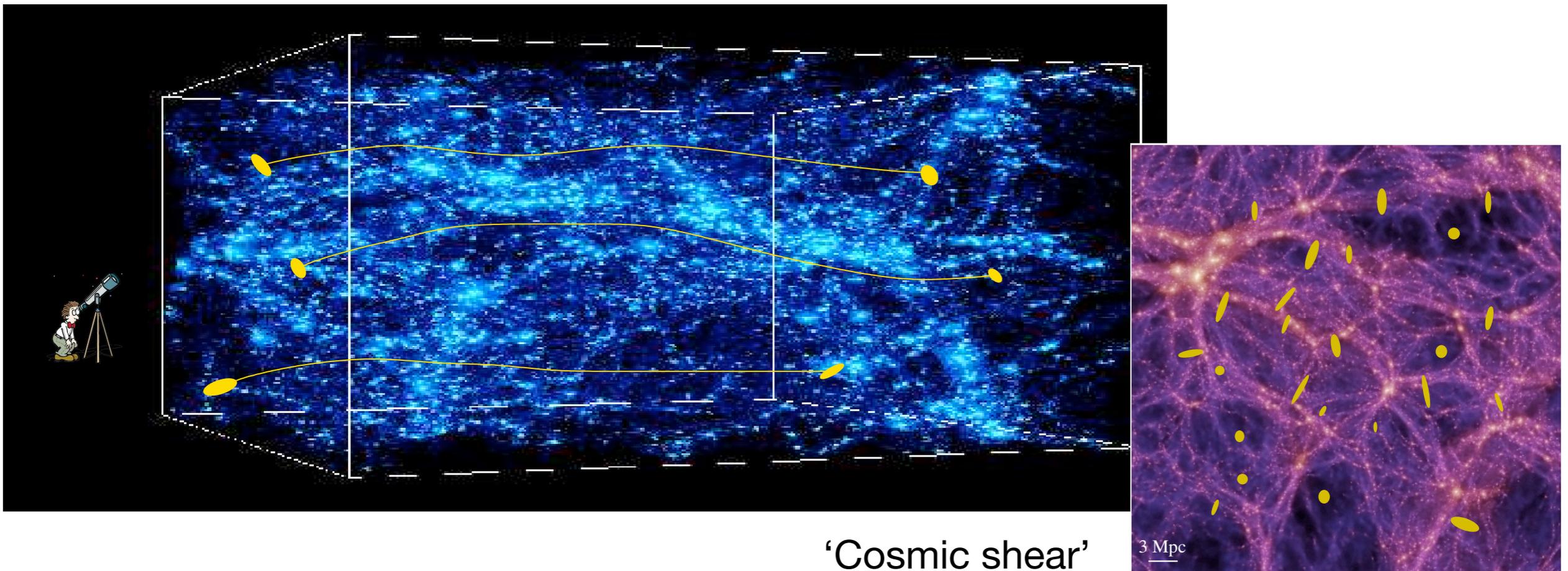
Structure formation



- Structure formation on large scales depends on cosmological parameters
- Structures consist mainly (80%) of invisible dark matter
- Galaxies as dark-matter tracers requires complex physics

Gravitational lensing as probe of the large-scale structure

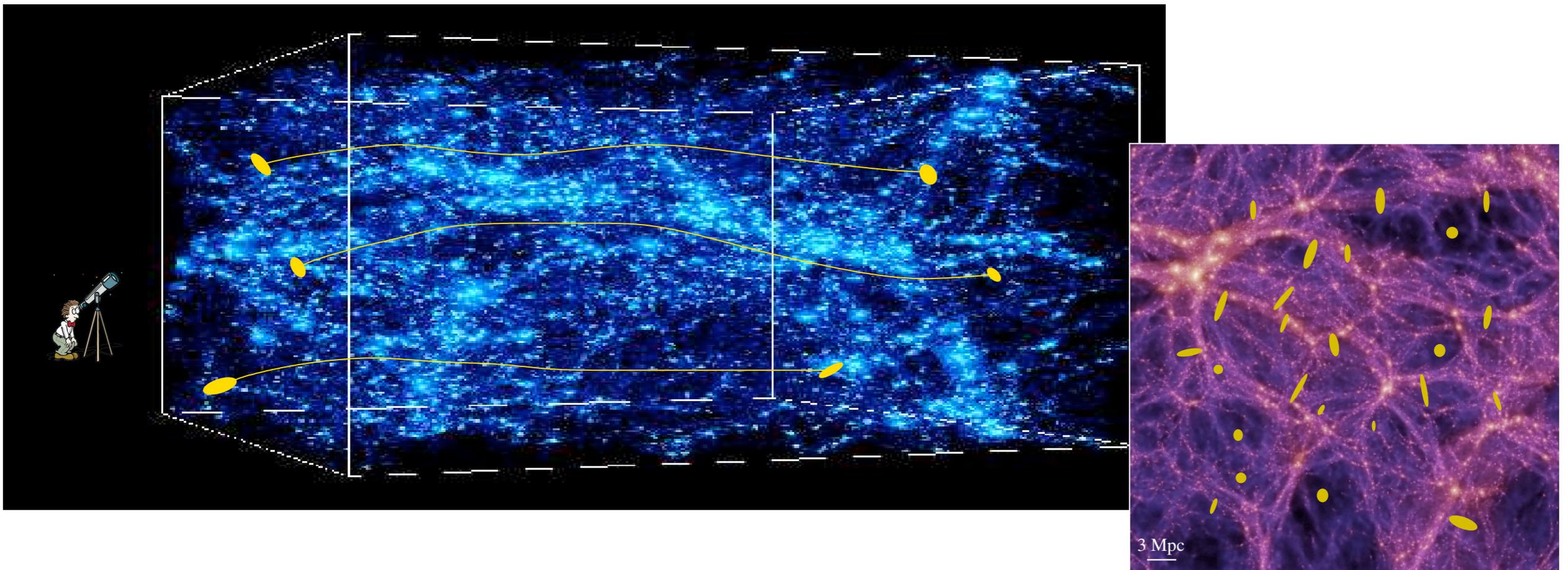
- Light from distant galaxies is continuously deflected along its path through the inhomogeneous Universe
- Light bundles are differentially ‘lensed’ by tidal matter field
- Galaxy images are coherently distorted → shape correlations, depending on statistical properties of (projected) large-scale structure



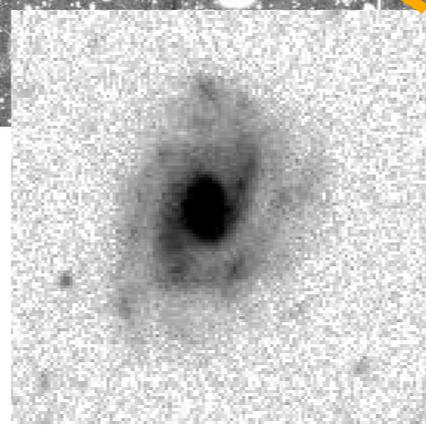
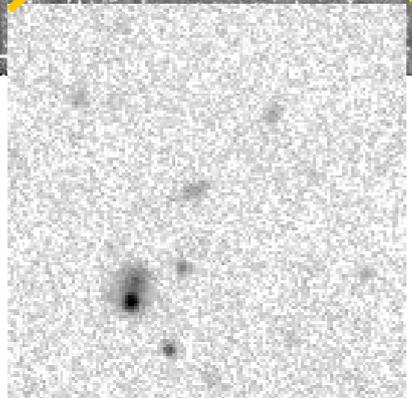
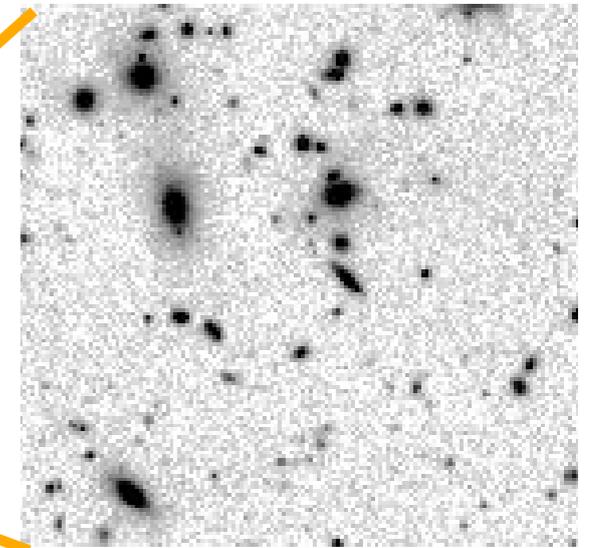
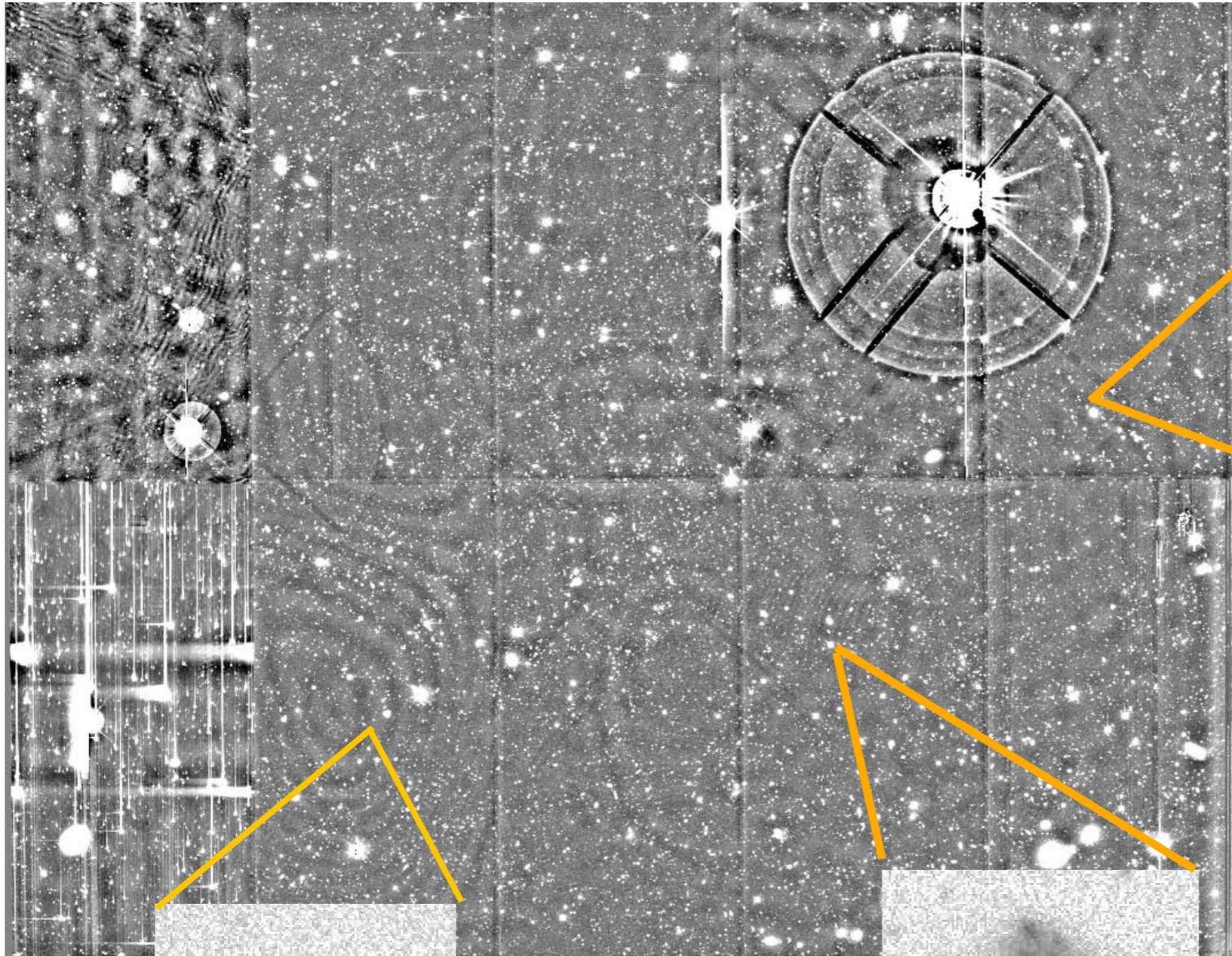
‘Cosmic shear’

Weak cosmological lensing ...

- probes structures @ $z=0.3 \dots 1$, where accelerated expansion sets in
- probes both **growth of structure** and **geometry** of Universe \rightarrow can distinguish between **modified gravity** and **dark energy**

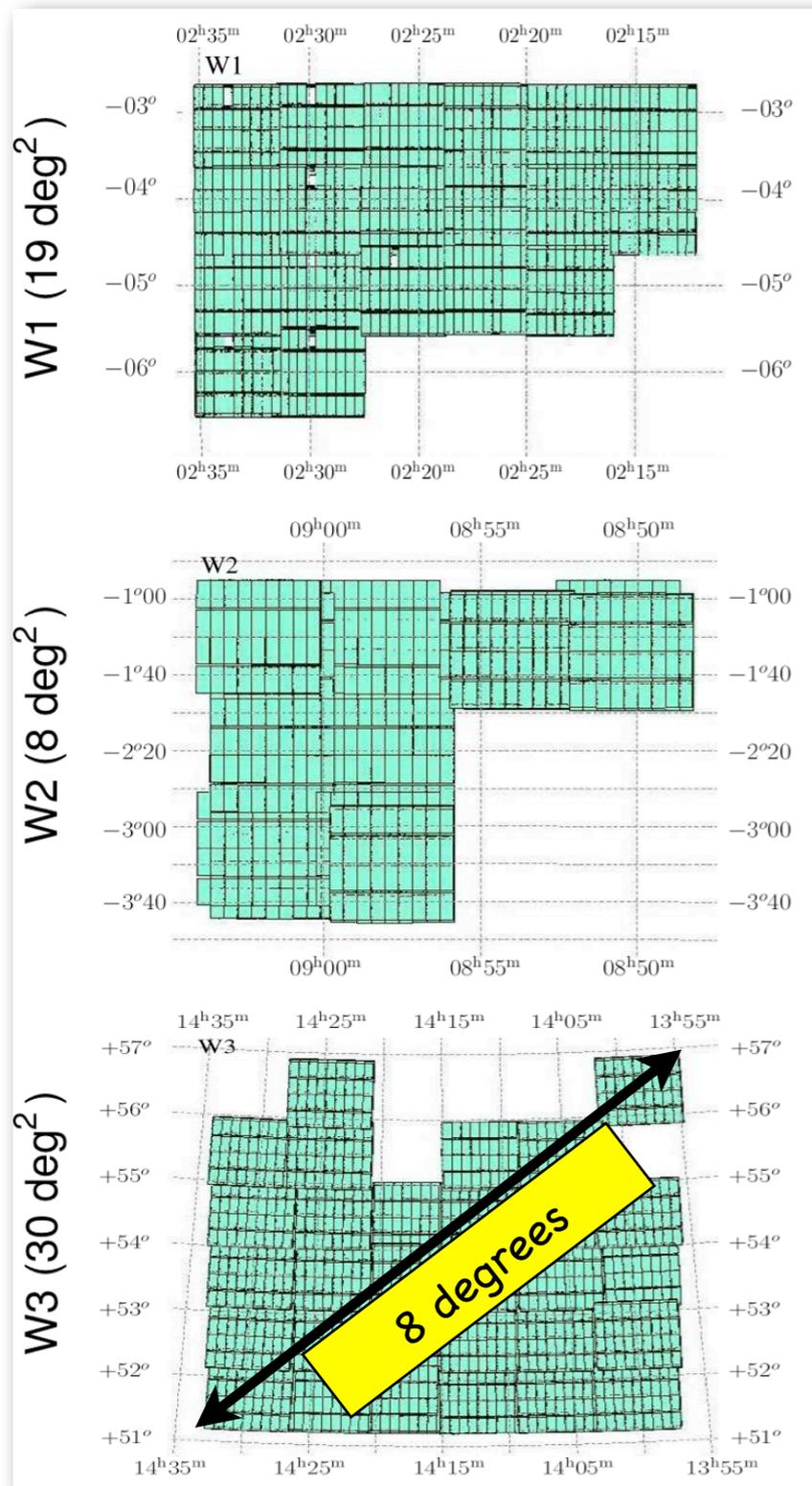


Weak lensing observations



- Gravitational lensing effect much smaller than intrinsic galaxy shapes or instrumental/atmospheric distortions
- Need to estimate accurate shapes of millions of galaxy images

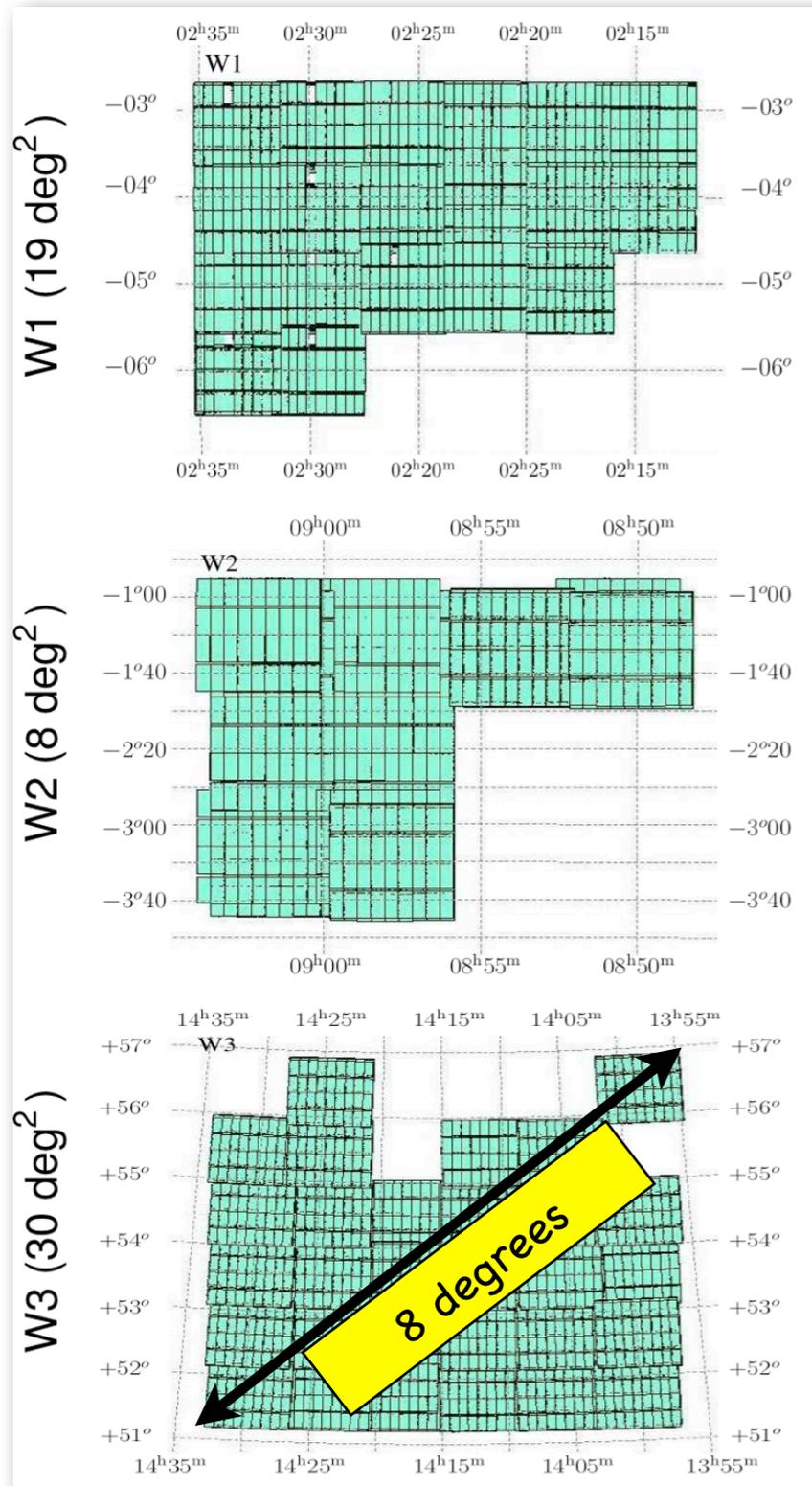
Weak lensing data



- Canada-France Hawaii Telescope (CFHT):
3.6m telescope
MegaCam: 1 deg² field of view (4x full moon)
- Legacy Survey (LS): 500 nights (2003-2008),
five optical bands, final area 170 deg²
- 3rd data release: 57 deg², 2 million galaxies,
only one band

[Fu, Hoekstra, Semboloni, MK et al. 2008]

Weak lensing data



- Canada-France Hawaii Telescope (CFHT): 3.6m telescope
MegaCam: 1 deg² field of view (4x full moon)
- Legacy Survey (LS): 500 nights (2003-2008), five optical bands, final area 170 deg²
- 3rd data release: 57 deg², 2 million galaxies, only one band

SUPRIME-33	SUBARU/Suprime	33 deg ²	R	R=26	2003-?
VIKING	VISTA/	1500 deg ²	zYJHK	$i_{AB}=22.9$	2007-2010
Dark Energy Survey DarkCam	CTIO DECam VISTA	5000 deg ² ~10,000 deg ²	griz ugriz	$i_{AB}=24.5$ $i_{AB}=24.$	2009-2014 2010-2014
HyperCam	SUBARU/ Suprime	~3500 deg ²	Vis.	?	>2012?
SNAP/JDEM	Space	100/1000/ 5000 deg ²	Vis.+NIR	-	>2013
DUNE	Space	~20000 deg ²	ugriz+NIR?	$i=25.5$	~2015?
LSST	Ground TBD	20000 deg ²	ugrizy	$i_{AB}=26.5$	>2014
Dome-C	SouthPole	? deg ²	?	?	~2012?

CFHTLS lensing data used for:

- Modified gravity:

Yukawa-, Uzan-Bernardeau potentials [Doré, Martig, Mellier, MK et al. 2009]
no deviation from GR for 0.04 Mpc... 10 Mpc

Constraints on gravitational slip ($\psi \neq \varphi$) [Daniel, Caldwell, Cooray & Melchiorri 2008]
DGP models excluded at 2σ [Thomas, Abdalla & Weller 2008]

- Dark energy constraints [MK, Benabed, Guy, Astier et al. 2009, Wraith, MK, Benabed, Cappé et al. 2009]

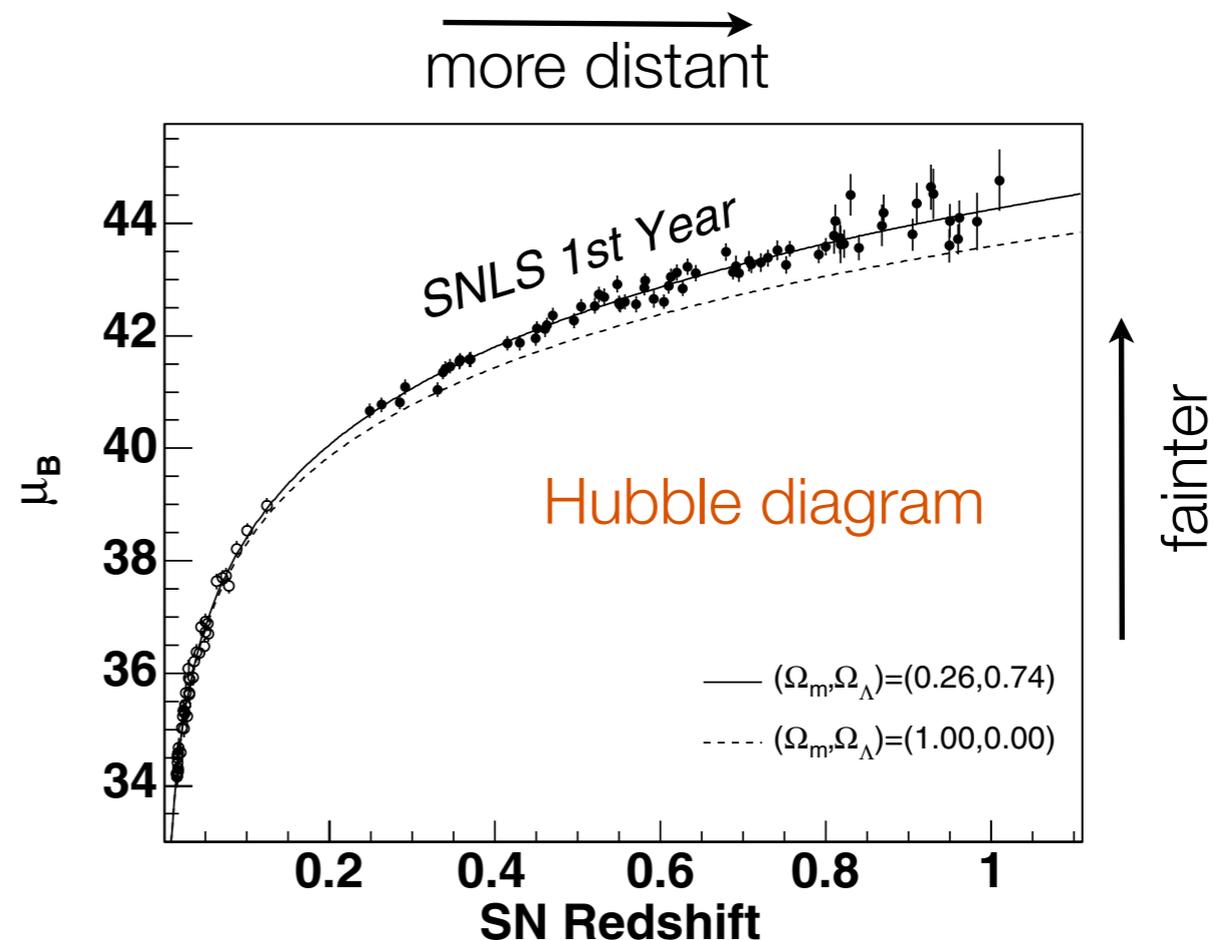
no deviation from Λ

- Neutrino masses [Terenio, Schimd, Uzan, MK et al. 2009, Ichiki, Takada & Takahashi 2009]

$\sum m < 0.54 \text{ eV}$

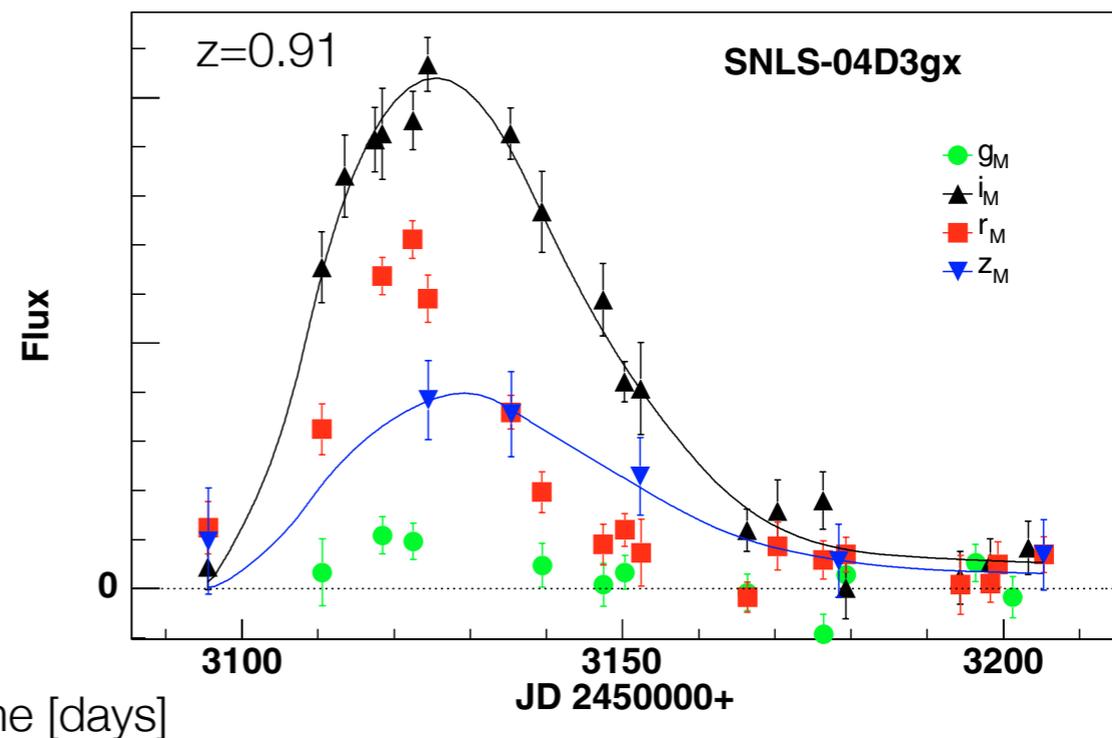
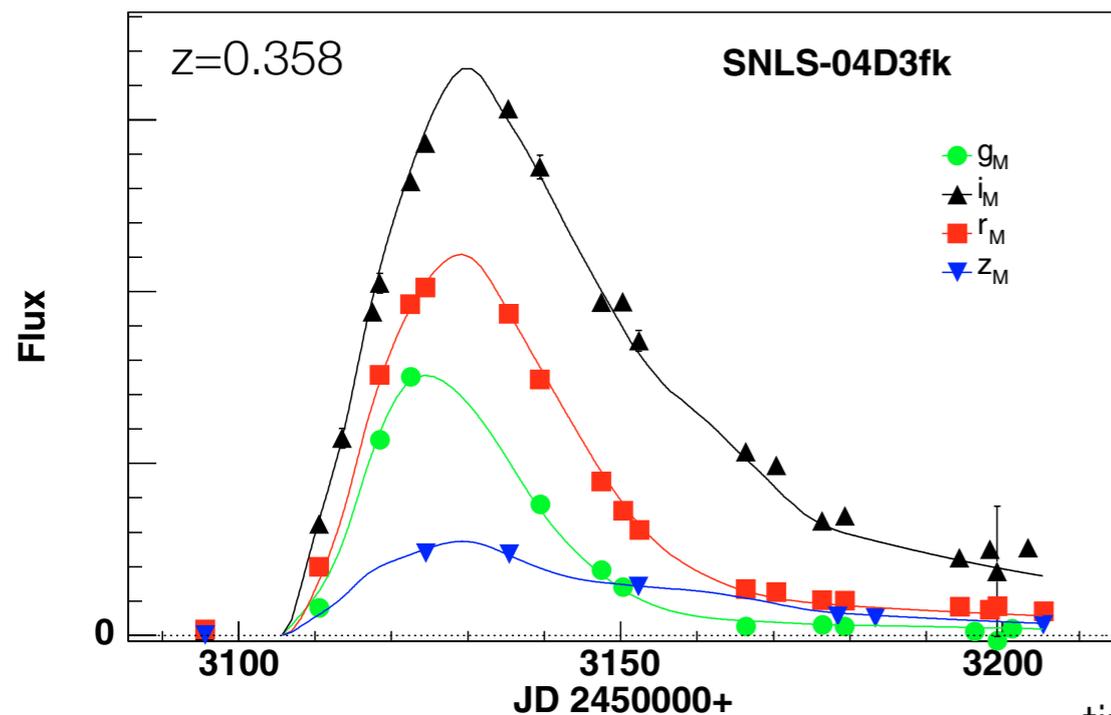
Supernovae of type Ia (SNIa)

- SNIa are thermo-nuclear explosions of a white dwarf with 1.4 solar masses
- They are standard candles: having universal intrinsic luminosity, observed luminosity only depends on distance
- Distance as function of redshift depends on expansion history of Universe



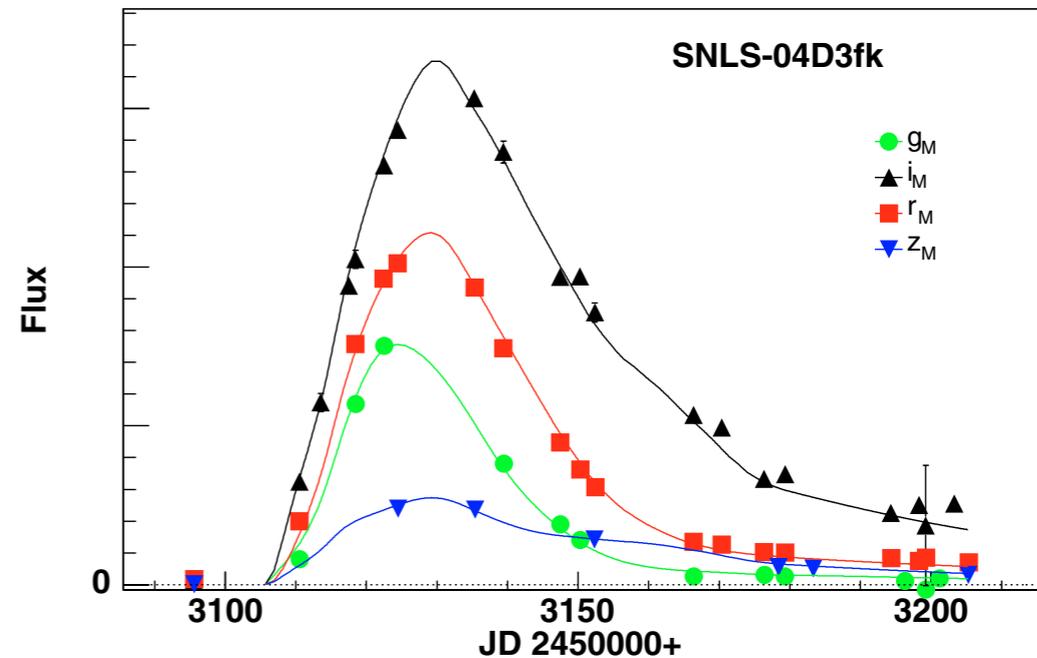
SN Ia data

- SNLS: Supernova Legacy Survey [Astier et al. 2006]
- 1st year data: 71 distant (+ 44 nearby SNe)
- Imaging: CFHT in 5 optical bands, 4 deg²
- Spectroscopy follow-up (for redshift, type): VTL, Gemini, Keck (8m class telescopes)

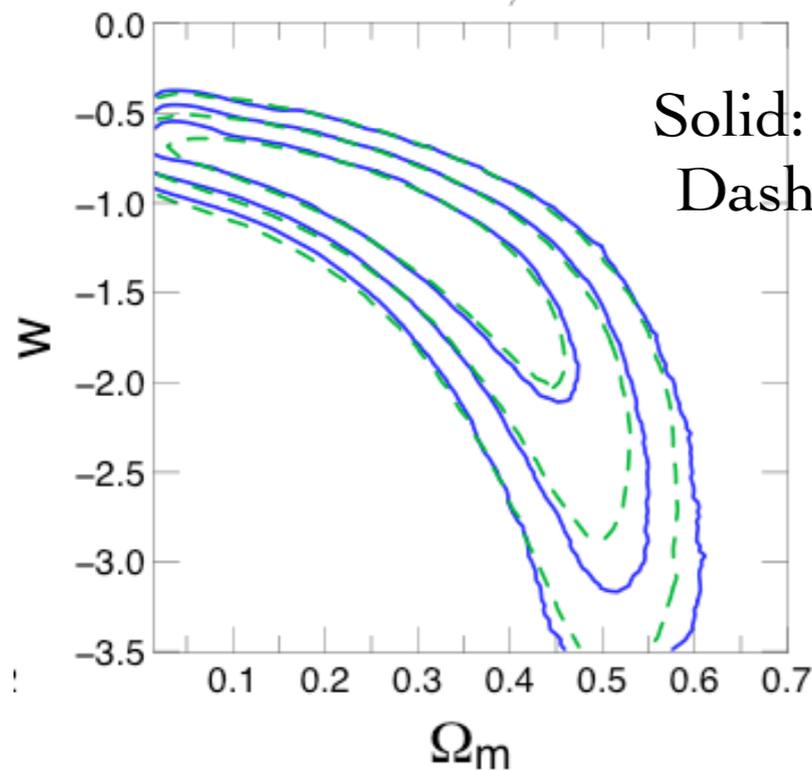


SN Ia systematics: photometry

- Uncertainties in photometry
 - wrong distance estimate
 - biased cosmological parameters



**Error bars
underestimated
by 10%-20%**



Solid: with systematics.
Dashed: ignoring sys.

with systematics

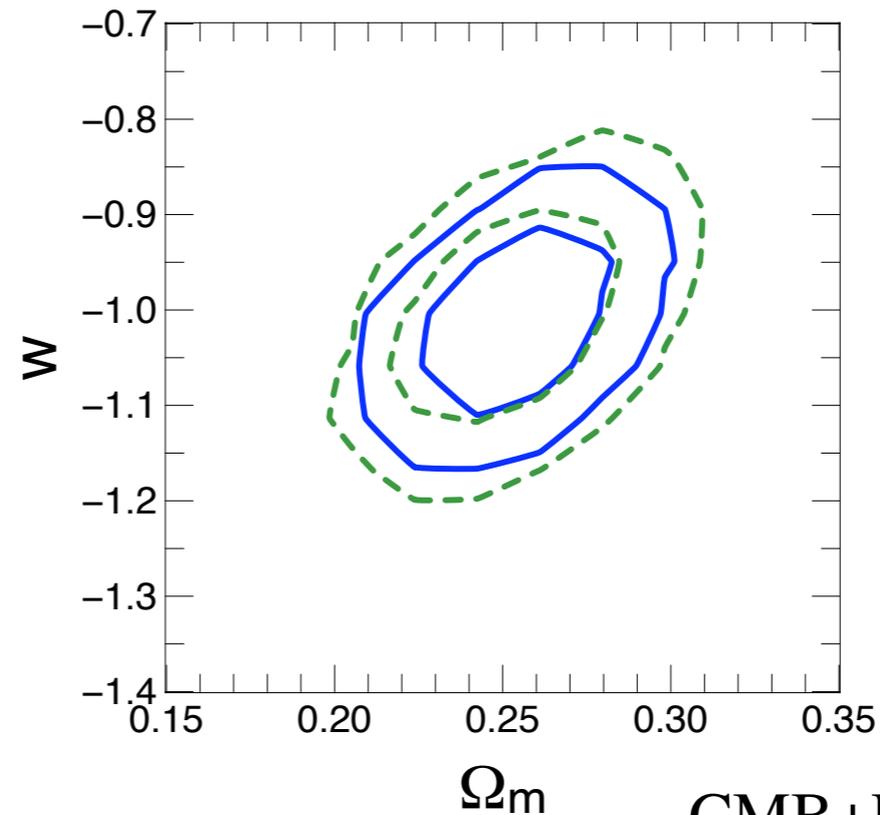
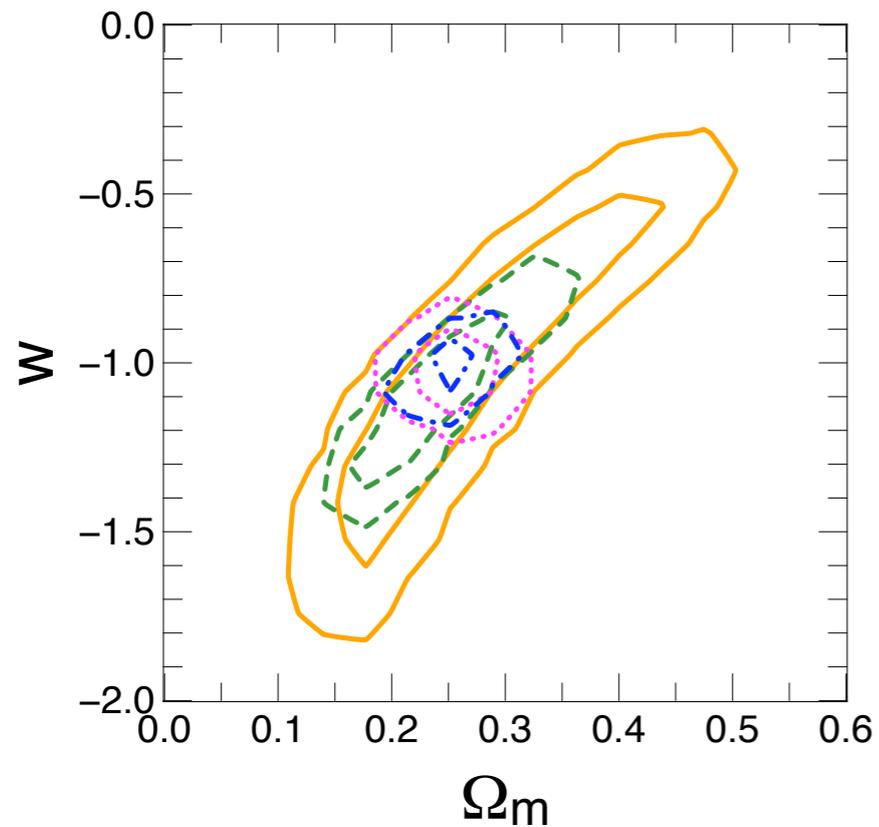
ignoring systematics

$$w(\Omega_m = 0.25)$$

$$-1.00^{+0.12}_{-0.12}$$

$$-1.01^{+0.09}_{-0.10}$$

Joint constraints on dark energy



— CMB
 - - - CMB+Lens
 ····· CMB+SN
 - · - CMB+Lens+SN

CMB+Lens+SN

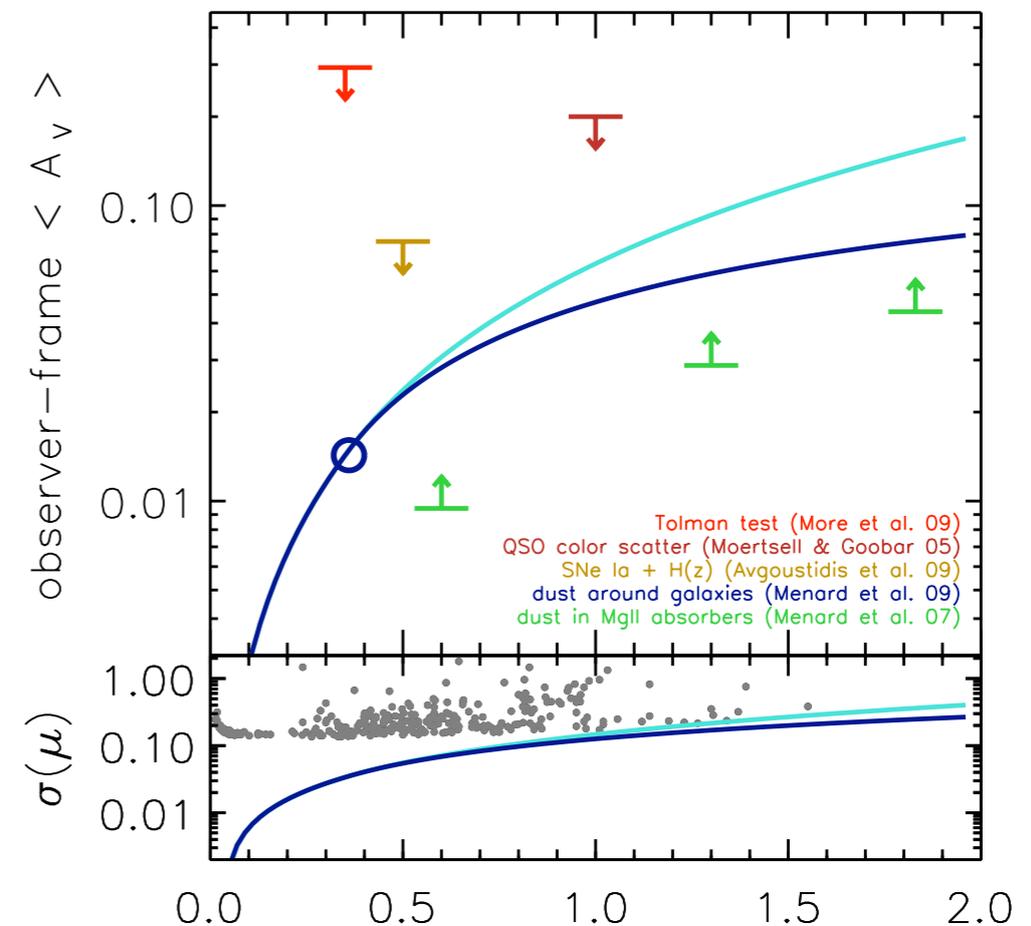
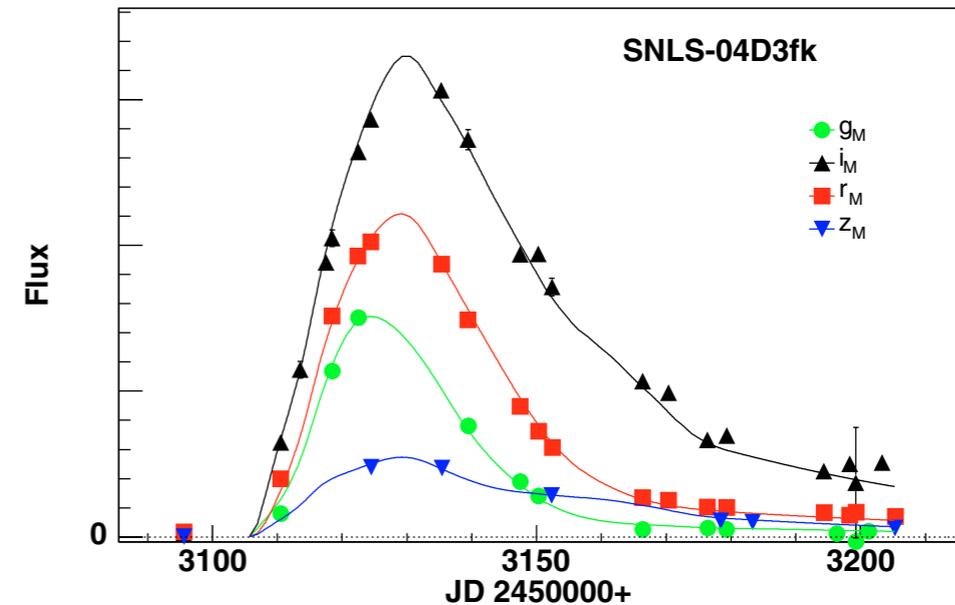
— ignoring systematics
 - - - with systematics

	CMB	SNIa	BAO	lens	Ly α	clust	gal	w
MK et al. 2009	x	x		x				$-0.18 < 1+w < 0.12$
Mantz et al. 2009	x	x	x			x		$-0.08 < 1+w < 0.04$ (68%)
Seljak et al. 2005	x	x			x		x	$-0.08 < 1+w < 0.10$
Komatsu et al. 2008	x	x	x					$-0.11 < 1+w < 0.14$
Jarvis et al. 2006	x	x		x				$-0.10 < 1+w < 0.27$
Wang & Mukherjee 2006	x	x					x	$-0.17 < 1+w < 0.16$

SN Ia systematics: dust absorption

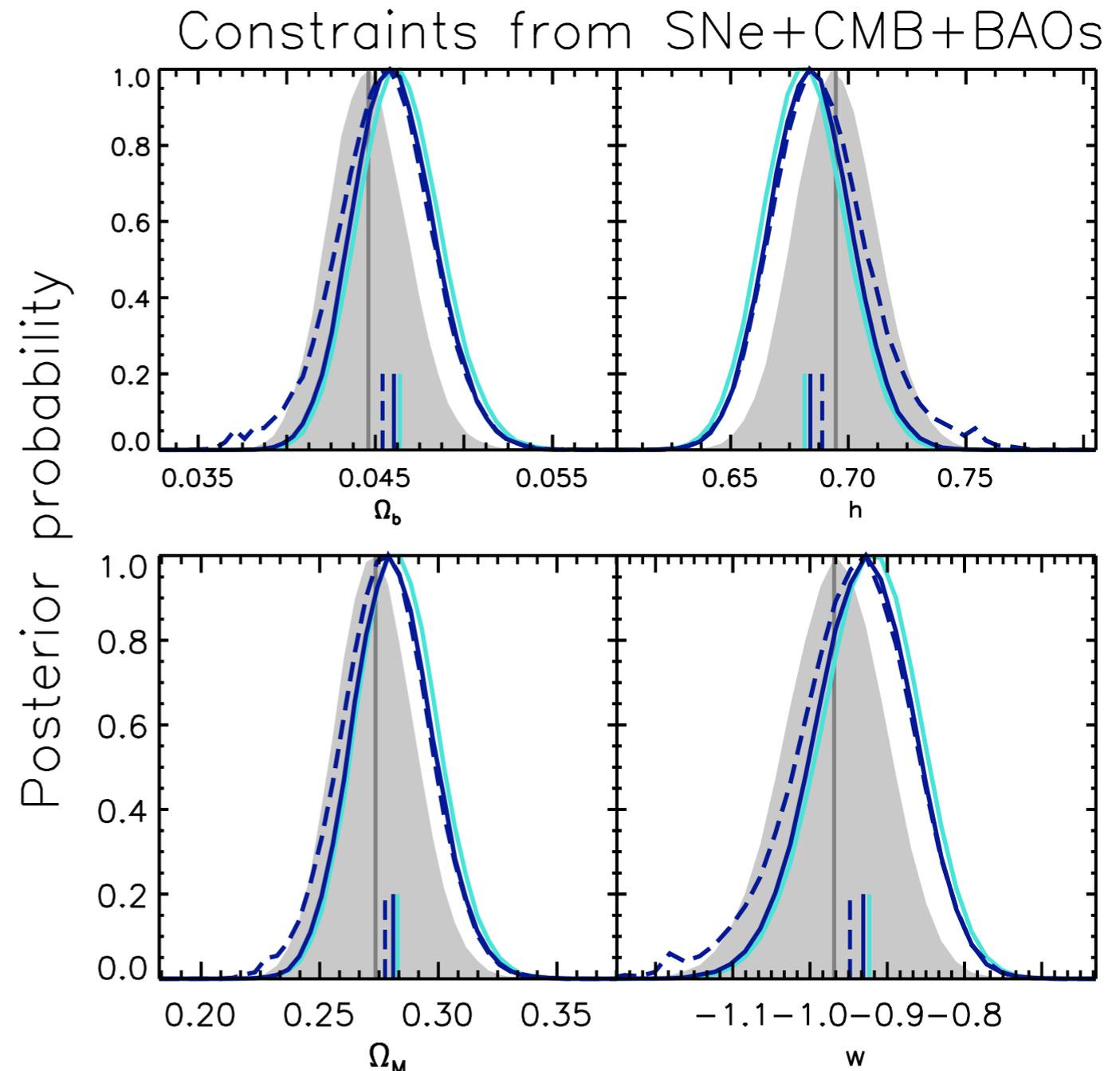
- Dust (in Milky Way, inter-galactic medium, SN host galaxy) absorbs light, SN Ia dimmer, has to be corrected for
- More absorption at shorter wavelengths (bluer bands)
- Linear correction:

$$\Delta(\text{brightness}) = \beta \times \text{color}$$
 β depends on dust properties
- Up to now:
 - color correction due to **one** dust comp.
 - inter-galactic medium neglected



SNIa systematics: dust absorption

- $\beta = 2.0 \dots 2.5$ up to now
- Menard et al. 2009:
 $\beta_{\text{IGM}} = 4.9 \pm 2.6$
- Ignoring this dust component leads to shifts in cosmological parameters
- $\Delta w = 0.02 - 0.03$, 25% to 30% of statistical error
- In future:
 - correction object by object
 - infrared less affected



[Menard, MK, Scranton 2009]

Model selection

- Traditional parameter estimation:
Q: For a specific model with n parameters which is the most likely (best-fit) parameter and confidence interval given the data?
- Model selection:
Q: Which of two or more models with parameters n_1, n_2, \dots is the most likely to fit the data?
- Examples in cosmology:
 - ★ cosmological constant Λ **vs.** dark energy **vs.** modified gravity
 - ★ flat **vs.** curved
 - ★ Primordial fluctuations: scale-free ($n_s=1$) **vs.** $n_s=\text{const}$ **vs.** running $n_s(k)$
- Other applications (Cluster profile reconstruction, exo-planets, ...)

Bayesian evidence

- Bayes' theorem

$$p(m, \theta | d) = \frac{\mathcal{L}(d | \theta, m) \pi(\theta | m)}{E(d | m)}$$

Likelihood Prior
 ↓ ↓
 Posterior ↑
 Evidence

m : model
 d : data
 θ : model parameter

Posterior is normalised

$$E(d | m) = \int d^n \theta \mathcal{L}(d | \theta, m) \pi(\theta | m)$$

- Bayes factor

$$B_{12} = \frac{E(d | m_1)}{E(d | m_2)}$$

- Ratio for two models m_1 and m_2 :

$$\frac{p(m_1 | d)}{p(m_2 | d)} = B_{12} \frac{\pi(m_1)}{\pi(m_2)}$$

Jeffreys' scale

$ \log_{10} B_{12} $	Odds	Strength
0 ... 0.5	1 ... 3	weak
0.5 ... 1	3 ... 10	substantial
1 ... 2	10 ... 100	strong
>2	>100	decisive

Approximations to the Evidence

- BIC (Bayesian Information Criterion) [Schwarz 1987]

$$\text{BIC} = -2 \ln \mathcal{L}_{\max} + k \ln N_{\text{data}}$$

likelihood @ maximum penalty for large parameter space
(Occam's razor)

(Similar: AIC, DIC)

Problem: Penalty independent whether parameters constrained by data or not

- Laplace approximation: likelihood Gaussian, priors large and uniform
[Lazarides, Ruiz de Austri & Trotta 2004, Heavens, Kitching & Verde 2007]

$$E \approx (2\pi)^{n/2} |F|^{-1/2} (\Delta\theta_1 \dots \Delta\theta_n)^{-1} \mathcal{L}_{\max}$$

volume allowed by data initial volume (prior)

Occam's razor

Laplace: priors might be small (physical parameter boundaries)

Fisher matrix not good approx.

Monte-Carlo methods

- MCMC?
Chain stays around high-likelihood, large regions of parameter space under-sampled.
- New method: PMC (Population MonteCarlo) [Cappé et al. 2004, 2007; Wraith, MK et al. 2009]
- Efficient integration over posterior:

$$\int d^n \theta h(\theta) \mathcal{L}(\theta) \pi(\theta)$$

$h(\theta)$	$= 1 :$	evidence
$h(\theta)$	$= \theta :$	mean
$h(\theta)$	$= 1_{68\%} :$	confidence region

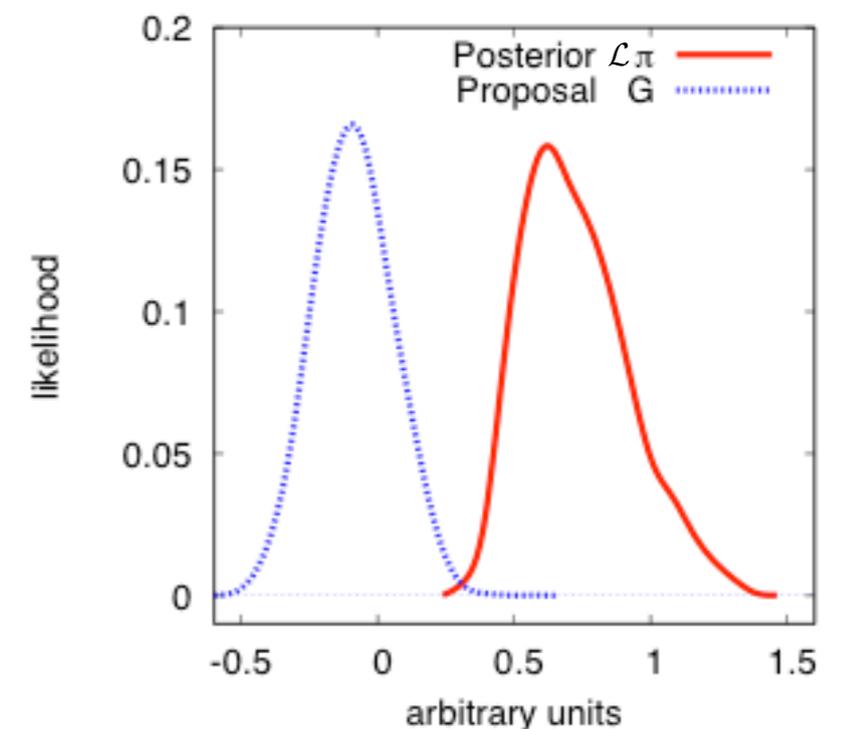
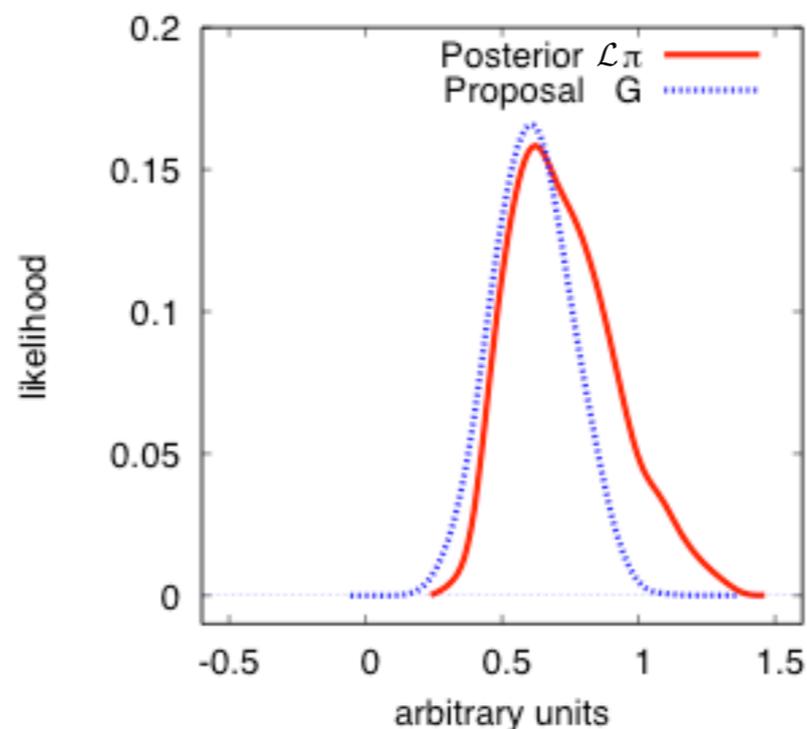
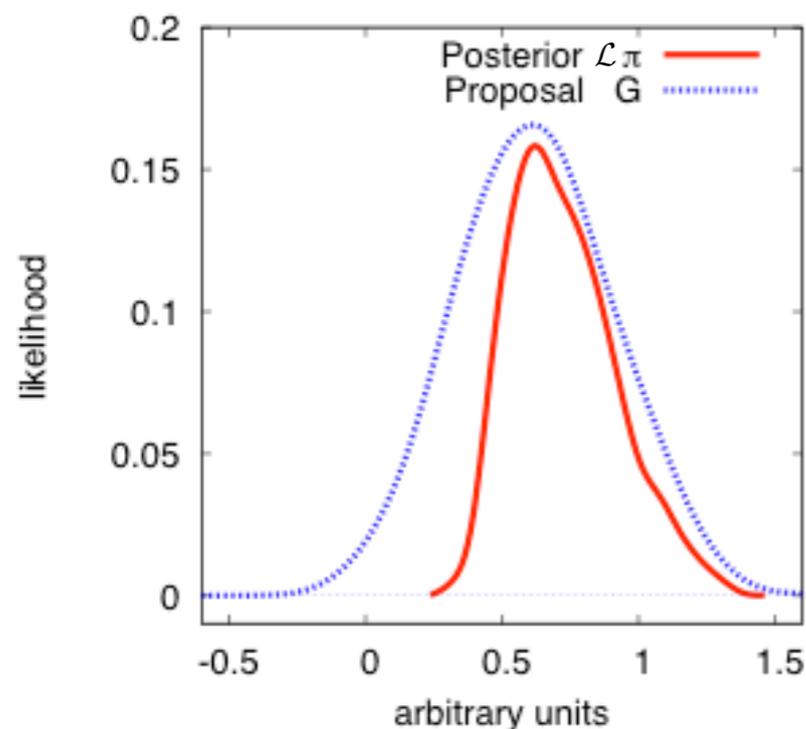
Importance sampling

- Rewriting the integral:

$$\int d^n \theta h(\theta) \mathcal{L}(\theta) \pi(\theta) = \int d^n \theta h(\theta) \frac{\mathcal{L}(\theta) \pi(\theta)}{G(\theta)} G(\theta)$$
$$= \frac{1}{N} \sum_{\theta_i \sim G} h(\theta_i) \frac{\mathcal{L}(\theta_i) \pi(\theta_i)}{G(\theta_i)} = \sum_{\theta_i \sim G} h(\theta_i) \bar{w}_i$$

normalised
importance weights
↓

- G : Proposal distribution, easy to sample from (mixtures of Gauss, Student-t, ...)

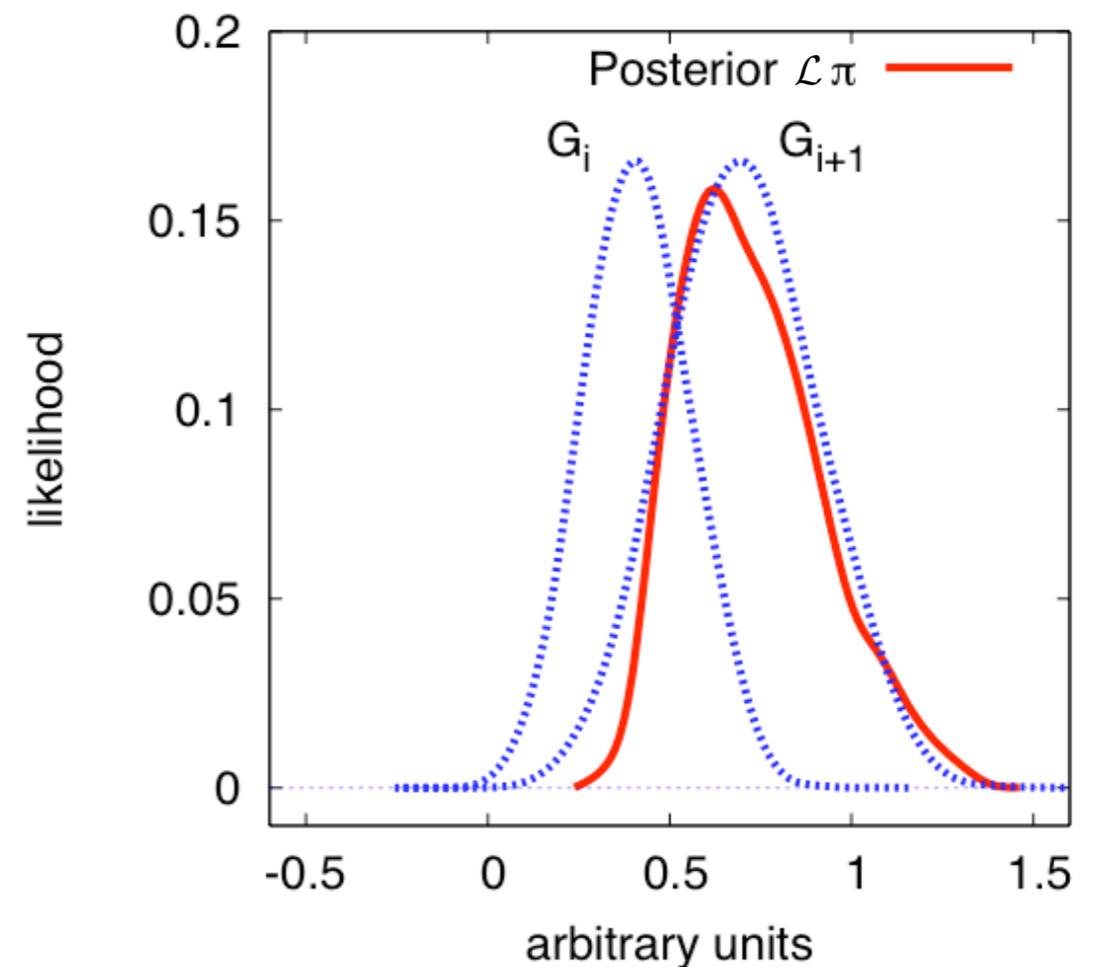


Population MonteCarlo (PMC)

- Importance sampling performs poorly if proposal far from posterior
- Solution: adaptive importance sampling aka Population MonteCarlo
[Cappé et al. 2004, 2007]
- Iterative update of proposal $G_i \rightarrow G_{i+1}$
- Stop iterations when proposal and posterior ‘close enough’:
Kullback-Leibler divergence

$$K = \int d^n \theta \log \left[\frac{\mathcal{L}(\theta)\pi(\theta)}{G(\theta)} \right] \mathcal{L}(\theta)\pi(\theta)$$

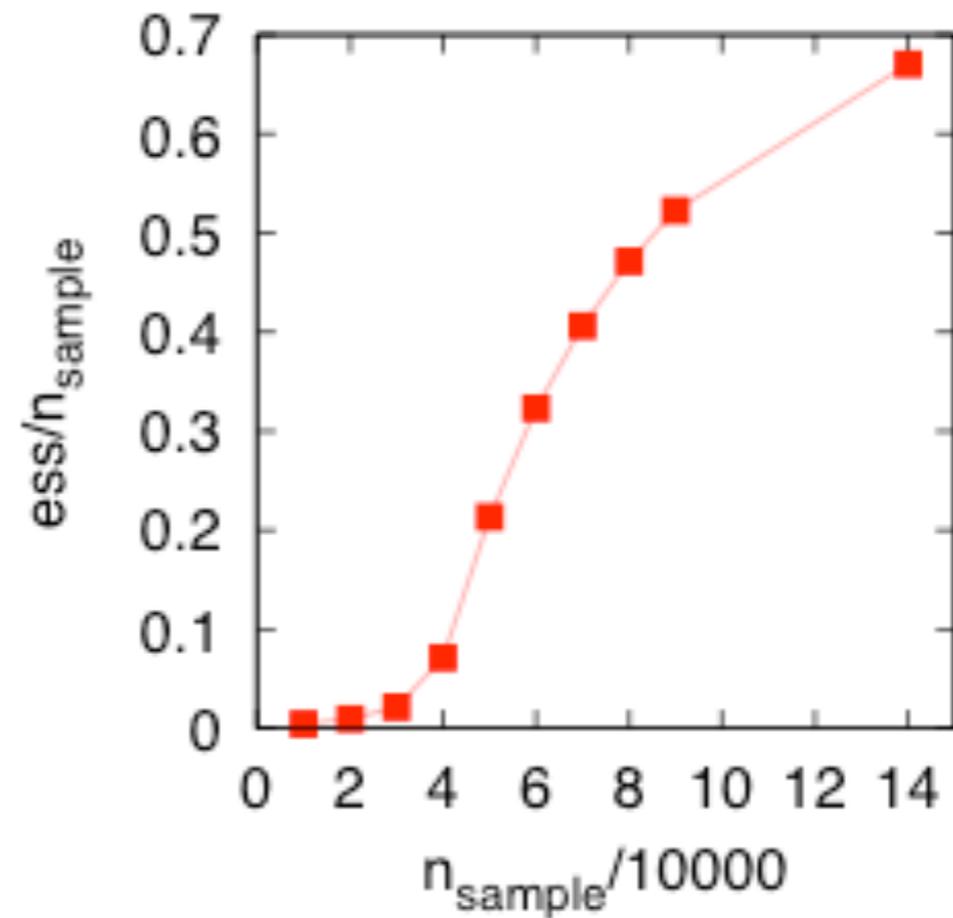
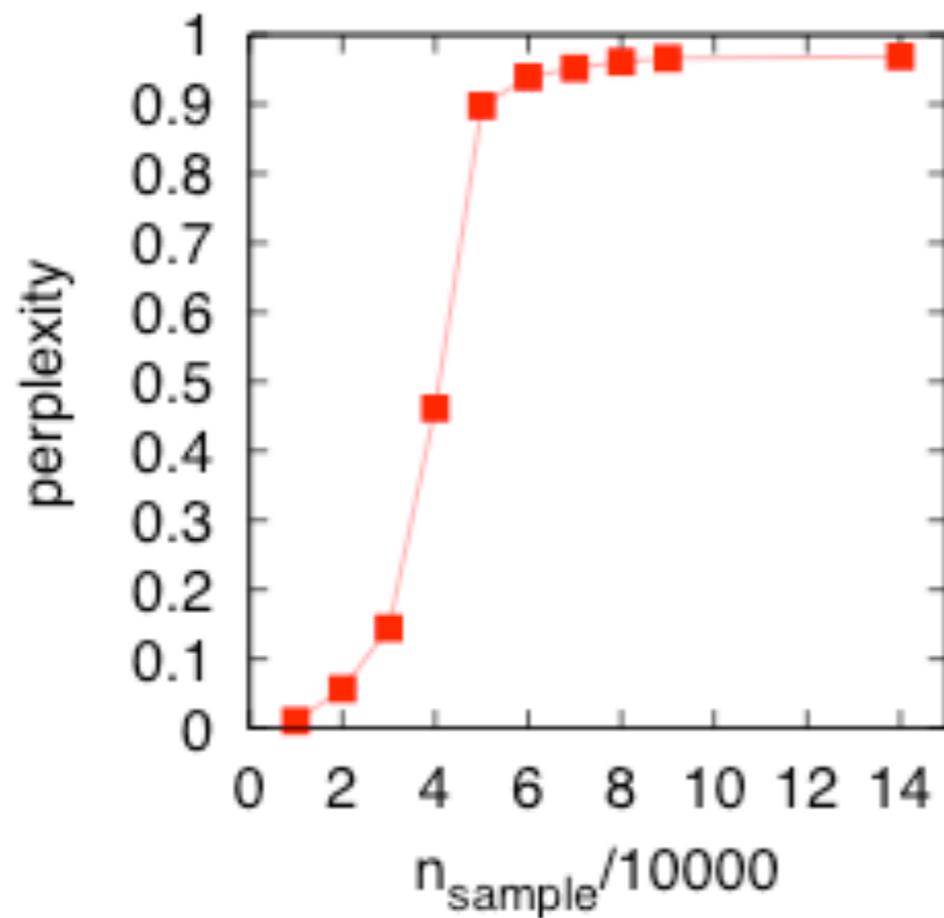
$$K = \int \log \left[\frac{\mathcal{L}(\theta)\pi(\theta)}{G(\theta)} \right] \frac{\mathcal{L}(\theta)\pi(\theta)}{G(\theta)} G(\theta) d\theta \approx \sum_{\theta_i \sim G} \log[\bar{w}_i] \bar{w}_i$$



PMC Performance

- Perplexity $p = \exp[-K]/N; \quad p = 0 \dots 1$

WMAP5 posterior, flat Λ CDM model, 6 parameters

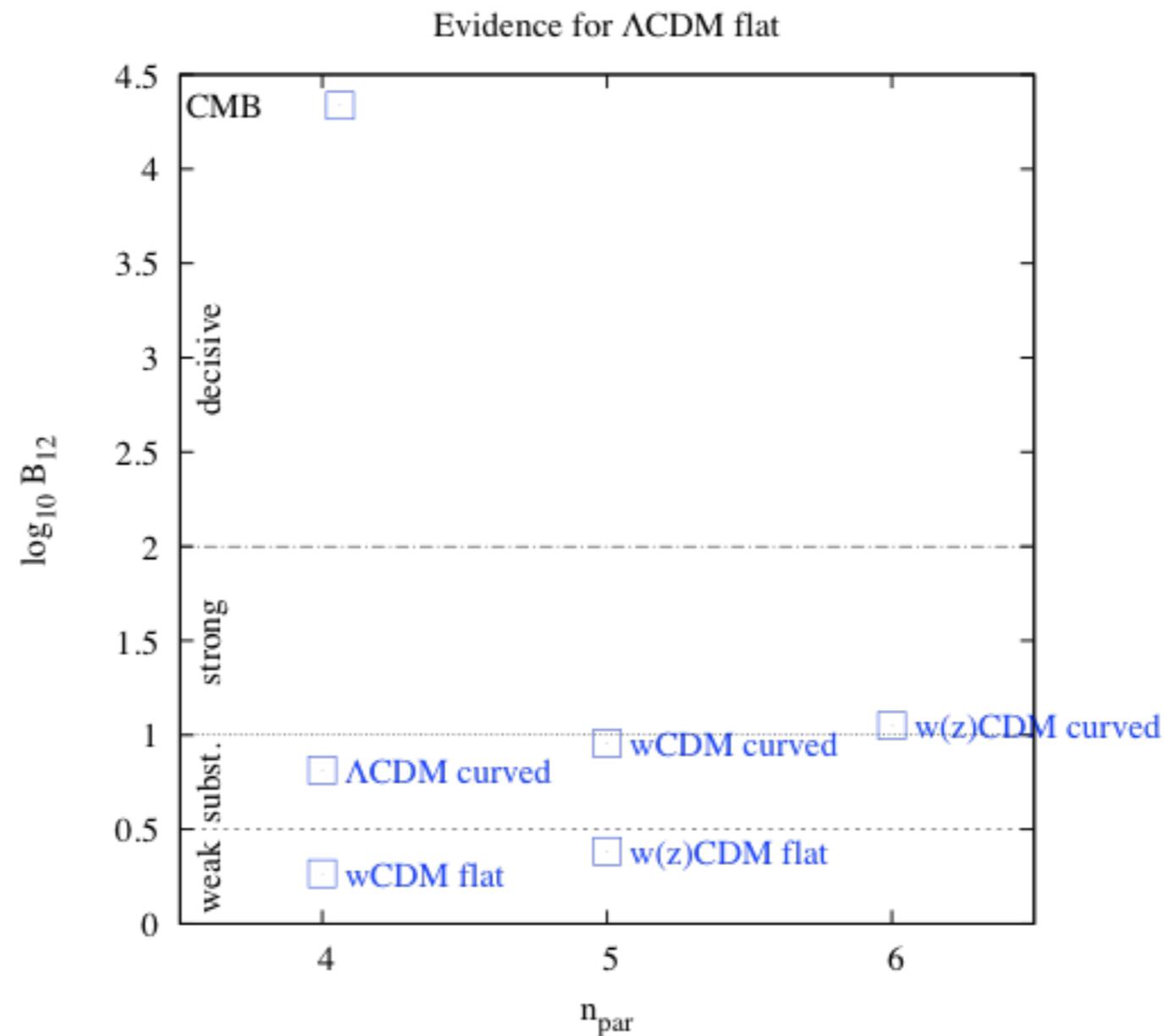


10 iterations

[Wraith, MK et al . 2009]

CMB+SNIa+BAO: Dark energy, curvature

- Base model: flat Λ CDM, $n_{\text{par}}=3$ (Ω_m, Ω_b, h)
Data: pure geometrical probes (WMAP5 distance priors, SNIa, BAO)

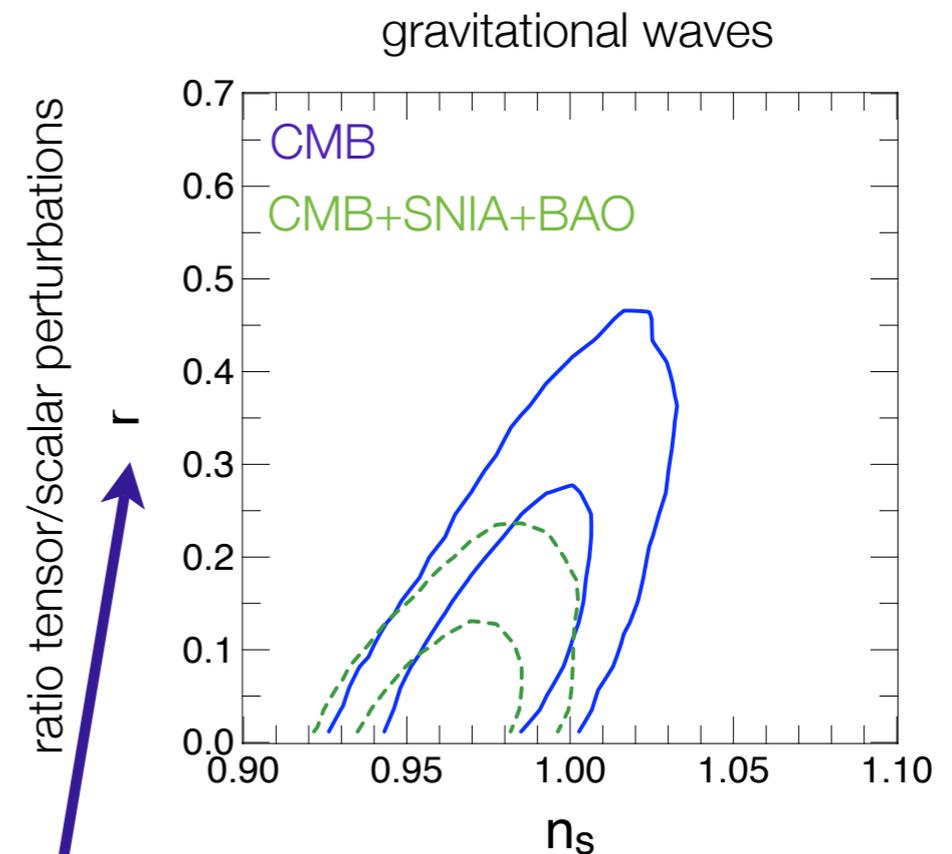
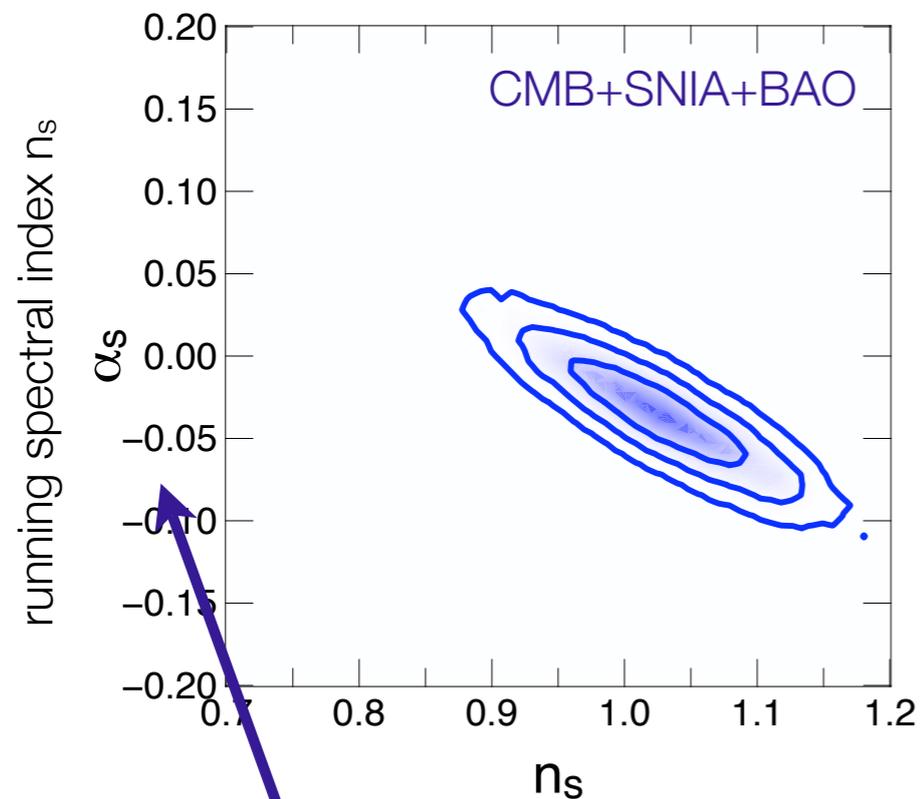


[MK, Wraith et al. in prep]

CMB+SNIa+BAO: Primordial perturbations

Primordial matter power spectrum:

$$P_{\delta}(k) \propto k^{n_s}$$



Model	n_{par}	$\log E$
$n_s = 1(\text{HZ})$	5	0.396
$n_s = \text{const}$	6	0.000
running	7	0.528
tensor	7	-1.599

Jeffreys' scale

$ \log_{10} B_{12} $	Odds	Strength
0 ... 0.5	1 ... 3	weak
0.5 ... 1	3 ... 10	substantial
1 ... 2	10 ... 100	strong
>2	>100	decisive

Summary & Conclusions

- Need multi-probe experiments to probe recent accelerated expansion of the Universe
 - ★ Control of systematics (e.g. dust absorption in SNIa, need large-scale structure observations)
 - ★ Distinguish between MoGR and dark energy
- Bayesian evidence
 - ★ powerful method to compare models
 - ★ important to design future experiments

