Talk-21

Asymptotic stability of stationary wave for damped wave equation with non-convex convection term

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We consider the initial-boundary value problem for damped wave equations with a nonlinear convection term in the half line. In the case where the flux is convex, it is shown by Ueda [3] that the solution tends to the corresponding stationary wave. In this talk, we show that even for a quite wide class of flux functions which are not necessarily convex, such the stationary wave is asymptotically stable. The proof is given by a technical L^2 -weighted energy method which derived by Hashimoto-Matsumura [2].

References:

- T.-P. Liu, A. Matsumura and K. Nishihara, Behavior of solutions for the Burgers equations with boundary corresponding to rarefaction waves, SIAM J. Math. Mech. 29 (1998), 293-308.
- [2] I. Hashimoto and A. Matsumura, Large-time behavior of solutions to an initial boundary value problem on the half line for scalar viscous conservation law, Methods Appl. Anal. 14 (2007), 45–60.
- [3] Y. Ueda, Asymptotic stability of stationary waves for damped wave equations with a nonlinear convection term, Adv. Math. Sci. Appl. 18 (2008), 329–343.